Scope and Sequence: A Pathway to Learning Algebra 1

Topic/Unit	Suggested Ti	ime Frame:
Chapter 1: Expressions and Functions	Quarter # 1	5 weeks
Priority Cluster and Standard(s):	Supporting Star	ndards:
 A1.N-Q.A: Reason quantitatively and use units to solve problems. A1.N-Q.A.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays, include utilizing real-world context. A1.A-SSE.A: Interpret the structure of expressions. A1.A-SSE.A.1 Interpret expressions that represent a quantity in terms of its context. a. Interpret parts of an expression, such as terms, factors, and coefficients. b. Interpret expressions by viewing one or more of their parts as a single entity. A1.A-SSE.A.2 Use structure to identify ways to rewrite numerical and polynomial expressions. Focus on polynomial multiplication and factoring patterns. A1.A-CED.A.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. A1.F-IF.A.1 Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x). 	 A1.N-RN.B: Use prop A1.N-RN.B.3 rational; that th irrational; and number is irrat A1.N-Q.A: Reason qu A1.N-Q.A: Reason qu A1.N-Q.A.2 E modeling. Incl A1.N-Q.A.3 C measurement v A1.F-IF.B Interpret ft A1.F-IF.B. Interpret ft A1.F-IF.B. S F applicable, to t A1.A-REI.D Represe A1.A-REI.D Represe A1.A-REI.D.I the set of all it curve, which c 	 perties of rational and irritation numbers Explain why the sum or product of two rational numbers is he sum of a rational number and an irrational number is hat the product of a nonzero rational number and an irrational tional. uantitatively and use units to solve problems. Define appropriate quantities for the purpose of descriptive lude problem-solving opportunities utilizing real-world context. Choose a level of accuracy appropriate to limitations on when reporting quantities utilizing real world context. Sunctions that arise in applications in terms of the context Relate the domain of a function to its graph and, where the quantitative relationship it describes. ent and solve equations and inequalities graphically. 10 Understand that the graph of an equation in two variables is ts solutions plotted in the coordinate plane, often forming a could be a line.

• A1.F-IF.A.2 Evaluate a function for inputs in the domain, and interpret statements that use function notation in terms of a context.

A1.F-IF.B Interpret functions that arise in applications in terms of the context

• A1.F-IF.B.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Include problemsolving opportunities utilizing real-world context. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step).

A1.F-IF.C Analyze functions using different representations

- A1.F-IF.C.7 Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step).
- A1.F-IF.C.8 Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.

a. Use the process of factoring and completing the square of a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.

Essential Question(s):

How can mathematical ideas be represented?

How do you choose appropriate levels of accuracy?

How can a decision be made about the level of accuracy needed or desired for a real-world measurement?

Why is it helpful to have several different representations of the same relation?

- Why are functions useful representations?
- Why are graphs useful representations?

	L
Key Concept(s):	Key Vocabulary:
I can	• accuracy
Minimally Proficient	algebraic expression
• Write verbal expressions for algebraic expressions. <i>MP</i>	• base
• Write algebraic expressions for verbal expressions. MP	• coefficient
• Recognize the properties of equality and identity properties. MP	• coordinate system
• Recognize the Commutative and Associative Properties. MP	dependent variable
• Define appropriate quantities for descriptive modeling. MP	• domain
	• end behavior
Partially Proficient	• exponent
• Use the Distributive Property to evaluate expressions PP	• function
• Use the Distributive Property to simplify expressions. PP	• independent variable
• Represent relations PP	• Intercept
• Interpret graphs of relations PP	• like terms
• Determine whether a relation is a function. PP	• line symmetry
 Find linear equations <i>PP</i> 	• metric
	• ordered pair
Proficient	• order of operations
• Evaluate numerical expressions by using the order of	• origin
operations P	• power
• Evaluate algebraic expressions by using the order of operations	• range
<i>p</i>	• reciprocal
• Choose appropriate levels of accuracy P	• relation
 Interpret intercents and symmetry of graphs of functions P 	• relative maximum
 Interpret increasing and decreasing behavior 	• relative minimum
extrema and end behavior of graphs of functions P	• simplest form
entrema, and end condition of graphs of functions.	• term
	• variables
	• vertical line test
	end behavior

Topic/Unit		Suggested T	ime Frame:
Chapter 2: Linear Equations		Quarter # 1	3 weeks
Priority Cluster and Standard(s):	Su	pporting Sta	indards:
A1.A-CED.A Create equations that describe numbers or relationships.			
• A1.A-CED.A.1 Create equations and inequalities in one			
variable and use them to solve problems. Include problem-			
solving opportunities utilizing real-world context. Focus on			
linear, quadratic, exponential and piecewise-defined functions			
(limited to absolute value and step).			
• A1.A-CED.A.4 Rearrange formulas to highlight a quantity of			
interest, using the same reasoning as in solving equations. For			
example, rearrange Ohm's law			
V = IR to highlight resistance R.			
AI.A. DELA 1 Evaluin and inequalities in one variable.			
• AI.A-REI.A.I Explain each step in solving linear and audretic equations as following from the equality of numbers			
asserted at the previous step, starting from the assumption that			
the original equation has a solution. Construct a viable			
argument to justify a solution method			
• A1.A-RELB.3 Solve linear equations and inequalities in one			
variable, including equations with coefficients represented by			
letters.			
Essential Question(s):			
Why is it helpful to represent the same mathematical idea in different way	ys?		
Why is it helpful to represent a mathematical idea using an equation?			
How can you represent mathematical relationships using ratios and proport	rtior	ns?	

Key Concept(s):	Key Vocabulary:
I can	• consecutive integers
Minimally Proficient	• dimensional analysis
• Translate sentences into equations. <i>MP</i>	• equivalent equations
• Translate equations into sentences. <i>MP</i>	• extremes
	• formula
<u>Partially Proficient</u>	• identity
• Use algebra tiles to model solving equations. PP	• linear equation
• Solve equations by using addition and subtraction. PP	• literal equation
• Solve equations by using multiplication and division. PP	• means
• Solve equations involving more than one operation. PP	• multi-step equations
• Solve equations involving consecutive integers. PP	• number theory
• Compare ratios. PP	• proportion
• Solve proportions. PP	• rate
	• ratio
<u>Proficient</u>	• scale
• Solve equations with the variable on both sides. P	• scale model
• Solve equations involving grouping symbols. <i>P</i>	• solve an equation
• Evaluate absolute value expressions. P	• unit analysis
• Solve absolute value equations. P	• unit rate

Topic/Unit		Suggested Time Frame:		
Ch 3: Linear and Nonlinear Functions		Quarter # 2	3 weeks	
Priority Cluster and Standard(s):	Su	pporting Sta	andards:	
 A1.N-Q.A: Reason quantitatively and use units to solve problems. A1.N-Q.A.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays, include utilizing real-world context. A1.A-CED.A Create equations that describe numbers or relationships. A1.A-CED.A.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. A1.A-REI.D Represent and solve equations and inequalities graphically. A1.A-REI.D IO Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve, which could be a line. A1.F-IF.B.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Include problem-solving opportunities utilizing real-world context. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). A1.F-IF.B.6 Calculate and interpret the average rate of change of a continuous function (presented symbolically or as a table) on a closed interval. Estimate the rate of change from a graph. Include problem-solving opportunities utilizing real-world context are a continuous function (presented symbolically or as a table) on a closed interval. Estimate the rate of change from a graph. Include problem-solving opportunities utilizing real-world context are problem-solving opportunities utilizing real-world context. 	A1.	F-IF.B Interpret • A1.F-IF.A.3 recursively, v	functions that arise in applications in terms of the context Recognize that sequences are functions, sometimes defined whose domain is a subset of the integers.	

piecewise-defined functions (limited to absolute value and step).

A1.F-IF.C Analyze functions using different representations

• A1.F-IF.C.7 Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.b Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step).

A1.F-LE.A Construct and compare linear, quadratic, and exponential models and solve problems.

- A1.F-LE.A.1 Distinguish between situations that can be modeled with linear functions and with exponential functions. a. Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.
- A1.F-LE.A.2 Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or input/output pairs.

A1.F-BF.A Build a function that models a relationship between two quantities.

• A1.F-BF.A.1 Write a function that describes a relationship between two quantities. Determine an explicit expression, a recursive process, or steps for calculation from real-world context. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step).

A1.F-BF.B Build new functions from existing functions.

• A1.F-BF.B.3 Identify the effect on the graph of replacing f(x) by f(x) + k, k f(x), and f(x+k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step).

Essential Question(s):

Why are graphs useful?

What are the benefits of having a model for a linear function?

Why is it helpful to have different ways to graph linear functions?

What can a linear graph tell you about the relationship that it represents?

Kay Concept(s).	Kov Vocabulary.
	Kcy v ocabulary.
Key Concept(s): Minimally Proficient I can Minimally Proficient I dentify linear equations, intercepts, and zero. MP Find the slope of a line. MP Find the slope of a line. MP Recognize arithmetic sequences. MP Partially Proficient Graph linear equations. PP Use rate of change to solve problems. PP Identify and graph step functions. PP Identify and graph piecewise-defined functions. PP Identify and graph reflections and dilations of absolute value functions. PP Identify and graph reflections and dilations of absolute value functions. PP Model linear functions. P Model linear functions. P Model real worl	Key Vocabulary: arithmetic sequence common difference constant constant function greatest integer function linear equation linear function piecewise-linear function rate of change root sequence slope slope-intercept form standard form step function transformations x-intercept y-intercept zero of a function
replacing $f(x)$ with $f(x) + k$ and $f(x - h)$ for positive and negative values. P	
• Identify the effects on the graphs of linear functions by replacing f(x) with af(x), f(ax), -af(x) and f(-ax) P	
• Relate arithmetic sequences to linear functions. P	

Topic/Unit		Suggested T	'ime Frame:	
Chapter 4: Equations of Linear Functions		Quarter # 2		2-3 weeks
Priority Cluster and Standard(s):	Su	pporting Sta	a	andards:
 Priority Cluster and Standard(s): A1.N-Q.A: Reason quantitatively and use units to solve problems. A1.N-Q.A.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays, include utilizing real-world context. A1.A-CED.A Create equations that describe numbers or relationships. A1.A-CED.A.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. A1.A-REI.D Represent and solve equations and inequalities graphically. A1.A-REI.D.10 Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve, which could be a line. A1.F-IF.B.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Include problem-solving opportunities utilizing real-world context. Key features include: intervents intervals where the function is increasing. 	Su	pporting Sta		ındards:
decreasing, positive, or negative; relative maximums and minimums. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and				
 step). A1.F-IF.B.6 Calculate and interpret the average rate of change 				
of a continuous function (presented symbolically or as a table) on a closed interval. Estimate the rate of change from a graph.				
context. Focus on linear, quadratic, exponential and piecewise- defined functions (limited to absolute value and step).				

A1.F-IF.C	Analyze	functions	using	different	representations
-----------	---------	-----------	-------	-----------	-----------------

• A1.F-IF.C.7 Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.b Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step).

A1.F-LE.A Construct and compare linear, quadratic, and exponential models and solve problems.

• A1.F-LE.A.2 Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or input/output pairs.

A1.F-BF.B Build new functions from existing functions.

• A1.F-BF.B.3 Identify the effect on the graph of replacing *f*(*x*) by *f*(*x*) + *k*, *k f*(*x*), and *f*(*x*+*k*) for specific values of *k* (both positive and negative); find the value of *k* given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step).

Essential Question(s):

Why is math used to model real-world situations?

When would a linear function be used to model a real-world situation?

How can you use a set of data to make predictions?

When would the inverse of a linear function be used to model a real-world situation?

Key Concept(s):	Key Vocabulary:
I can	• association
Minimally Proficient	• best-fit line
• Write an equation of a line in slope-intercept form given the	• bivariate data
slope and one point. MP	• causation
• Write an equation of a line in slope-intercept form given two	• constraint
points. MP	• correlation
• Use lines of fit to make and evaluate predictions. MP	• correlation coefficient
*	• inverse function
Partially Proficient	• inverse relation
• Investigate relationships between quantities by using points on	linear extrapolation
scatter plots. PP	• linear interpolation
• Write equations of lines in standard form and point-slope form.	linear regression
PP	• line of fit
• Write linear equations in different forms. PP	• median-fit line

 Write an equation of a line that passes through a given point, parallel to a given line. <i>PP</i> Write an equation of a line that passes through a given point, perpendicular to a given line. <i>PP</i> Write equations of best-fit lines using linear regression. <i>PP</i> Find the inverse of a relation. <i>PP</i> Find the inverse of a linear function. <i>PP</i> 	 parallel lines perpendicular lines point-slope form residual scatter plot standard form
 <u>Proficient</u> Distinguish between correlation and causation. <i>P</i> Draw the graph of an inverse relation by reflecting the overall graph in the line y = x. <i>P</i> 	

Topic/Unit	Suggested Time Frame:			
Chapter 5: Linear Inequalities	Quarter # 2	2-3 weeks		
Priority Cluster and Standard(s):	Supporting Sta	andards:		
 A1.A-CED.A Create equations that describe numbers or relationships. A1.A-CED.A.1 Create equations and inequalities in one variable and use them to solve problems. Include problemsolving opportunities utilizing real-world context. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). A1.A-REI.B Solve equations and inequalities in one variable. A1.A-REI.B.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. 	 A1.A-REI.D Repres A1.A-REI.D a half-plane, graph the sol intersection of 	sent and solve equations and inequalities graphically. 0.12 Graph the solutions to a linear inequality in two variables as excluding the boundary in the case of a strict inequality, and lution set to a system of linear inequalities in two variables as the of the corresponding half-planes.		
Essential Question(s):				
How are symbols useful in mathematics? What mathematical symbols do you know? Why is it important to understand what the symbols in a mathematical sem How are symbols used to write expressions, equations, and inequalities? How are graphs helpful when solving inequalities in two variables?	tence represent?			
Key Concept(s):	Key Vocabula	ry:		
I can <u>Minimally Proficient</u> Solve linear inequalities by using addition. <i>MP</i> Solve linear inequalities by using subtraction. <i>MP</i> Use algebra tiles to model and solve inequalities. <i>MP</i> Solve linear inequalities by using multiplication. <i>MP</i> Solve linear inequalities by using division. <i>MP</i> Graph linear inequalities on the coordinate plane. <i>MP</i> Solve inequalities by graphing. <i>MP</i>	 boundary closed half-p compound ir half-plane inequality intersection open half-pla union 	plane nequality ane		
 <u>Partially Proficient</u> Solve linear inequalities involving more than one operation. <i>PP</i> Solve linear inequalities involving the Distributive Property. <i>PP</i> Solve and graph absolute value inequalities (< and >) <i>PP</i> 				

Proficient

- Solve compound inequalities containing the word and, and graph their solution set. *P*Solve compound inequalities containing the word or, and graph their solution set. *P*
- Use a graphing calculator to investigate the graphs of inequalities. *P*

Topic/Unit	Suggested T	Time Frame:
Chapter 6:	Quarter #	3 weeks
Systems of Linear Equations and Inequalities	3	
Priority Cluster and Standard(s):	Supporting Sta	andards:
 A1.A-CED.A Create equations that describe numbers or relationships. A1.A-CED.A.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. A1.A-CED.A.3 Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context. A1.A-REI.D Represent and solve equations and inequalities graphically. A1.A-REI.D.11 Explain why the x-coordinates of the points where the graphs of the equations y=f(x) and y=g(x) intersect are the solutions of the equation f(x) =g(x); find the solutions approximately (e.g., using technology to graph the functions, make tables of values, or find successive approximations). Focus on cases where f(x) and/or g(x) are linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). 	 A1.A-REI.C Solve a A1.A-REI.C replacing one produces a synthematic synth	 systems of equations. 2.5 Prove that, given a system of two equations in two variables, e equation by the sum of that equation and a multiple of the other ystem with the same solutions. sent and solve equations and inequalities graphically. 2.10 Understand that the graph of an equation in two variables is its solutions plotted in the coordinate plane, often forming a could be a line. 2.12 Graph the solutions to a linear inequality in two variables as excluding the boundary in the case of a strict inequality, and ution set to a system of linear inequalities in two variables as the of the corresponding half-planes.
Essential Question(s):		
How can you find the solution to a math problem? What are the advantages of using technology to solve systems of equations What are the benefits of having different strategies for solving systems of o What are the advantages of using matrices to solve problems?	? equations?	

Key Concept(s):	Key Vocabulary:
 I can Minimally Proficient Determine the number of solutions a system of linear equations has. MP Determine the number of solutions a system of linear equations has. MP Solve systems of linear equations by graphing. PP Use a graphing calculator to graph and solve a system of equations. PP Solve systems of equations by using substitution. PP Solve systems of linear inequalities by graphing. PP Solve systems of equations by using elimination with addition. PP Solve systems of equations by using elimination with subtraction. PP Solve systems of equations by using elimination with multiplication. PP 	 augmented matrix consistent dependent dimension element elimination inconsistent independent matrix substitution system of equations system of inequalities
 <u>Proficient</u> Determine the best method for solving systems of equations. <i>P</i> Apply systems of equations. <i>P</i> Use matrices to solve systems of equations. <i>P</i> Apply systems of linear inequalities. <i>P</i> Solve real-world problems involving systems of equations. <i>P</i> 	

Topic/Unit		Suggested T	ime Frame:
Chapter 7:		Quarter #	2 L
Exponents and Exponential Functions		3	3 weeks
Priority Cluster and Standard(s):	Su	ເpporting Sta	andards:
 A1.A-SSE.A: Interpret the structure of expressions. A1.A-SSE.A.2 Use structure to identify ways to rewrite numerical and polynomial expressions. Focus on polynomial multiplication and factoring patterns. A1.A-CED.A Create equations that describe numbers or relationships. A1.A-CED.A.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. A1.A-RELD Represent and solve equations and inequalities graphically. A1.A-RELD.11 Explain why the x-coordinates of the points where the graphs of the equations y=f(x) and y=g(x) intersect are the solutions of the equation f(x) =g(x); find the solutions approximately (e.g., using technology to graph the functions, make tables of values, or find successive approximations). Focus on cases where f(x) and/or g(x) are linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). A1.F-IF.B.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Include problem-solving opportunities utilizing real-world context. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). 	A1	 N-RN.B: Use pro- A1.N-RN.B.: rational; that irrational; and irrational num. F-IF.A Understa A1.F-IF.A.3 recursively, v 	operties of rational and irritation numbers 3 Explain why the sum or product of two rational numbers is the sum of a rational number and an irrational number is d that the product of a nonzero rational number and an nber is irrational. nd the concept of a function and use function notation. Recognize that sequences are functions, sometimes defined whose domain is a subset of the integers.
 A1.F-BF.B Build new functions from existing functions. A1.F-BF.B.3 Identify the effect on the graph of replacing f(x) 			
by $f(x) + k$, $k f(x)$, and $f(x+k)$ for specific values of k (both			

positive and negative); find the value of <i>k</i> given the graphs.	
Experiment with cases and illustrate an explanation of the	
effects on the graph. Focus on linear, quadratic, exponential	
and piecewise-defined functions (limited to absolute value and	
step).	
A1.F-LE.A Construct and compare linear, quadratic, and exponential	
models and solve problems.	
• A1.F-LE.A.1 Distinguish between situations that can be	
modeled with linear functions and with exponential functions.	
a. Prove that linear functions grow by equal differences over	
equal intervals, and that exponential functions grow by equal	
factors over equal intervals.	
b. Recognize situations in which one quantity changes at a	
constant rate per unit interval relative to another.	
c. Recognize situations in which a quantity grows or decays by	
a constant percent rate per unit interval relative to another.	
• A1.F-LE.A.2 Construct linear and exponential functions,	
including arithmetic and geometric sequences, given a graph, a	
description of a relationship, or input/output pairs.	
A1.F-LE.B Interpret expressions for functions in terms of the situation	
they model.	
• A1.F-LE.B.5 Interpret the parameters in a linear or	
exponential function with integer exponents utilizing real	
world context	
Essential Question(s):	
How can you make good decisions? What factors affect good decision mathematical sectors affect and the sector of t	aking?
Why do you think it is important to simplify redical symposions?	-

Why do you think it is important to simplify radical expressions? How can mathematical models help you make good decisions? Summarize the transformations produced by performing various operations on the parent exponential function. How can being financially literate help you to make good decisions?

Key Concept(s):	Key Vocabulary:
 I can Minimally Proficient Multiply monomials using the properties of exponents. MP Simplify square roots by applying the Product and Quotient Properties of Square Roots. MP Add, subtract, and multiply radical expressions. MP Graph exponential functions. MP Identify data that display exponential behavior. MP Divide monomials using the properties of exponents. MP Partially Proficient Simplify expressions containing negative and zero exponents. PP Solve equations involving expressions with rational exponents. PP Write exponential functions by using a graph, a description, or two points. PP Identify and generate geometric sequences. PP 	 asymptote common ratio compound interest conjugates constant cube root exponential decay exponential equation exponential function exponential growth geometric sequence monomial negative exponent nth root order of magnitude radical expression radical exponent rationalizing the denominator recursive formula zero exponent
 <u>Proficient</u> Given the equation of an exponential function, predict how the dependent variable will change over an interval of the independent variable. <i>P</i> Evaluate and rewrite expressions involving rational exponents. <i>P</i> Identify the effects on the graphs of exponential functions by replacing f(x) with f(x) + k and negative values of h and k. <i>P</i> Identify the effects on the graphs of exponential functions by replacing f(x) with af(x) and f(ax) with positive and negative values of a. <i>P</i> Create equations and solve problems involving exponential growth and decay. <i>P</i> Transform and interpret expressions of exponential functions 	

- by applying the properties of exponents. *P*Relate geometric sequences to exponential functions. *P*Use a recursive formula to list terms in a sequence. *P*

Highly Proficient

• Write recursive formulas for arithmetic and geometric sequences. <i>HP</i>	

Topic/Unit	Sugges	sted 7	Time Frame:
Chapter 8: Polynomials	Quarte 4	er#	3weeks
Priority Cluster and Standard(s):	Supporti	ng Sta	andards:
 A1.A-SSE.A: Interpret the structure of expressions. A1.A-SSE.A.1 Interpret expressions that represent a quantity in terms of its context. a. Interpret parts of an expression, such as terms, factors, and coefficients. b. Interpret expressions by viewing one or more of their parts as a single entity. A1.A-SSE.A.2 Use structure to identify ways to rewrite numerical and polynomial expressions. Focus on polynomial multiplication and factoring patterns. A1.A-SSE.B Write expressions in equivalent forms to solve problems. A1.A-SSE.B.3 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. a. Factor a quadratic expression to reveal the zeros of the function it defines. 	A1.A-APR.A A1.A integy and n A1.A-APR.B A1.A availa by the and q A1.A-REI.C A1.A replac produ	Perfo -APR. ers, nam nultiplio Under -APR. able, an e polyn uadrati Solve -REI.C cing on acces a s	 rm arithmetic operations on polynomials. A.1 Understand that polynomials form a system analogous to the nely, they are closed under the operations of addition, subtraction, cation; add, subtract, and multiply polynomials. stand the relationship between zeros and factors of polynomials. B.3 Identify zeros of polynomials when suitable factorizations are d use the zeros to construct a rough graph of the function defined omial. Focus on quadratic and cubic polynomials in which linear c factors are available. systems of equations. C.5 Prove that, given a system of two equations in two variables, e equation by the sum of that equation and a multiple of the other ystem with the same solutions.
Essential Question(s):			
When could a nonlinear function be used to model a real-world situation? Why would you add, subtract, or multiply equations that represent real-world what are the advantages of using quadratic expressions for modeling?	orld situations	?	
Key Concept(s):	Key Voca	bula	ry:
I can	 binor degrad 	nial	nonomial
 Write polynomials in standard form. <i>MP</i> Add and subtract polynomials. <i>MP</i> Multiply a polynomial by a monomial. <i>MP</i> Use algebra tiles to find the product of two binomials. <i>MP</i> Find squares of sums and differences. <i>MP</i> Find the product of a sum and a difference. <i>MP</i> 	 degree degree differ factor factor FOIL leadin 	e of a p ence of ring ring by metho ng coef	polynomial Etwo squares grouping d ficient

perfect square trinomial

 <u>Partially Proficient</u> Solve equations involving the products of monomials and polynomials. <i>PP</i> Multiply binomials by using the FOIL method. <i>PP</i> Multiply polynomials by using the Distributive Property. <i>PP</i> Factor binomials using algebra tiles and a product mat. <i>PP</i> Use the Distributive Property to factor polynomials. <i>PP</i> Factor polynomials by grouping. <i>PP</i> Use algebra tiles to factor trinomials. <i>PP</i> 	 polynomial prime polynomial quadratic expression standard form of a polynomial trinomial
 <u>Proficient</u> Factor trinomials of the form x² + bx + c. <i>P</i> Factor trinomials of the form ax² + bx + c. <i>P</i> Factor binomials that are the difference of squares. <i>P</i> Factor trinomials that are perfect squares. <i>P</i> 	

Topic/Unit	Suggested Time Frame:
Chapter 9:	Quarter #
Quadratic Functions and Equations	4 4 weeks
Priority Cluster and Standard(s):	Supporting Standards:
 A1.A-SSE.B Write expressions in equivalent forms to solve problems. A1.A-SSE.B.3 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. a. Factor a quadratic expression to reveal the zeros of the function it defines. A1.A-CED.A Create equations that describe numbers or relationships. A1.A-CED.A.1 Create equations and inequalities in one variable and use them to solve problems. Include problemsolving opportunities utilizing real-world context. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). A1.A-CED.A.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. A1.F-IF.B. Interpret functions that arise in applications in terms of the context A1.F-IF.B.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Include problemsolving opportunities utilizing real-world context. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). A1.F-IF.B.6 Calculate and interpret the average rate of change of a continuous function (presented symbolically or as a table) on a closed interval. Estimate the rate of change form a graph. Include problem-solving opportunities utilizing real-world context. Focus on linear, quadratic, exponential and piecewise-defined functions (limited to absolute value and step). A1.F-IF.C Analyze functions using different representations 	 A1.A-REI.B Solve equations and inequalities in one variable. A1.A-REI.B.4 Solve quadratic equations in one variable. a. Use the method of completing the square to transform any quadratic equation in x into an equation of the form (x - k)² = q that has the same solutions. Derive the quadratic formula from this form. b. Solve quadratic equations by inspection (e.g., x² = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Focus on solutions for quadratic equations that have real roots. Include cases that recognize when a quadratic equation has no real solutions. A1.A-REI.C Solve systems of equations. A1.A-REI.C.5 Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions. A1.A-REI.C.6 Solve systems of linear equations in two variables. Include problem solving opportunities utilizing real-world context. A1.F-LE.A.3 Observe, using graphs and tables, that a quantity increasing exponentially eventually exceeds a quantity increasing linearly or quadratically.

• A1.F-IF.C.7 Graph functions expressed symbolically and show	
key features of the graph, by hand in simple cases and using	
technology for more complicated cases.b Focus on linear,	
quadratic, exponential and piecewise-defined functions (limited	
to absolute value and step).	
A1.F-BF.B Build new functions from existing functions.	
• A1.F-BF.B.3 Identify the effect on the graph of replacing $f(x)$	
by $f(x) + k$, $k f(x)$, and $f(x+k)$ for specific values of k (both	
positive and negative); find the value of k given the graphs.	
Experiment with cases and illustrate an explanation of the	
effects on the graph. Focus on linear, quadratic, exponential	
and piecewise-defined functions (limited to absolute value and	
step).	
A1.F-LE.A Construct and compare linear, quadratic, and exponential	
models and solve problems.	
• A1.F-LE.A.1 Distinguish between situations that can be	
modeled with linear functions and with exponential functions.	
a. Prove that linear functions grow by equal differences over	
equal intervals, and that exponential functions grow by equal	
factors over equal intervals.	
b. Recognize situations in which one quantity changes at a	
constant rate per unit interval relative to another.	
c. Recognize situations in which a quantity grows or decays by	
a constant percent rate per unit interval relative to another.	
• A1.F-LE.A.2 Construct linear and exponential functions,	
including arithmetic and geometric sequences, given a graph, a	
description of a relationship, or input/output pairs.	
Essential Question(s):	
Why do we use different methods to solve math problems?	
How can the graph of a quadratic function help you to solve the correspond	ding quadratic equation?
How is the symmetry of the graph of a quadratic function reflected in the s	solutions found by completing the square?

How do you know which method to use when solving a quadratic equation? When is it best to solve a system by graphing and when is it best to solve it by using substitution?

Key Concept(s):	Key Vocabulary:
 I can Minimally Proficient Identify key features of writing quadratic equations in vertex form. <i>MP</i> <u>Partially Proficient</u> Graph quadratic functions. <i>PP</i> Estimate solutions of quadratic equations by graphing. <i>PP</i> Solve quadratic equations by using the Square Root Property. <i>PP</i> Solve quadratic equations by factoring. <i>PP</i> Solve quadratic equations by completing the square. <i>PP</i> Solve quadratic equations by using the Quadratic Formula. <i>PP</i> Use the discriminant to determine the number of solutions of a quadratic equation. <i>PP</i> Solve systems of linear and quadratic equations by graphing. <i>PP</i> Identify linear, quadratic, and exponential functions from given data. <i>PP</i> 	 axis of symmetry completing the square discriminant double root maximum minimum parabola Quadratic Formula quadratic function standard form vertex vertex form
 <u>Proficient</u> Investigate the rate of change of a quadratic equation. <i>P</i> Solve quadratic equations by graphing. <i>P</i> Solve systems of linear and quadratic equations by using algebraic methods. <i>P</i> Write equations that model data. <i>P</i> Combine functions by using addition and subtraction. <i>P</i> Combine functions by using multiplication. <i>P</i> <u>Highly Proficient</u> Analyze the characteristics of graphs of quadratic functions. <i>HP</i> Apply translations to quadratic functions. <i>HP</i> 	

Topic/Unit		Suggested T	Time Frame:
Chapter 10: Statistics		Quarter # 4	2 weeks
Priority Cluster and Standard(s):	Su	ipporting Sta	andards:
 A1.S-ID.A Summarize, represent, and interpret data on a single count or measurement variable. A1.S-ID.A.1 Represent real-value data with plots for the purpose of comparing two or more data sets. A1.S-ID.A.2 Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets. A1.S-ID.A.3 Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of outliers if present. A1.S-ID.B Summarize, represent and interpret data on two categorical and quantitative variables A1.S-ID.B.5 Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data, including joint, marginal, and conditional relative frequencies. Recognize possible associations and trends in the data. A1.S-ID.C.8 Compute and interpret the correlation coefficient of a linear relationship. 	A1 to i	 S-CP.A Underst interpret data. A1.S-CP.A.I characteristic of other even A1.S-CP.A.2 understand th and <i>B</i> occurr characterizat A1.S-ID.B.6 and describe a. Fit a funct the context o b. Informally A1.S-ID.C.7 linear model A1.S-ID.C.9 	 and independence and conditional probability and use them a Describe events as subsets of a sample space using as of the outcomes, or as unions, intersections, or complements its. a Use the Multiplication Rule for independent events to hat two events A and B are independent if the probability of A ing together is the product of their probabilities, and use this ion to determine if they are independent. Represent data on two quantitative variables on a scatter plot, how the quantities are related. ion to the data; use functions fitted to data to solve problems in f the data. Focus on linear models. assess the fit of a function by plotting and analyzing esiduals. an the context of the data. Distinguish between correlation and causation.
How are statistics used in the real world?			
	1 1	1	

How can measures of center and percentile rank be used to analyze real-world data sets?

	· · · · · · · · · · · · · · · · · · ·
Key Concept(s):	Key Vocabulary:
 I can Minimally Proficient Represent sets of data by using measures of center. MP Represent sets of data by using percentiles. MP Represent data by using dot plots. MP Describe the shape of a distribution. MP Use the shapes of distribution to select appropriate statistics. MP Determine whether a discrete or continuous graphical representation is appropriate, and then create the bar graph or histogram. PP Calculate measures of spread. P Analyze data sets using statistics. P Determine the effect that transformations of data have on measures of central tendency and variation. P Compare data using measures of central tendency and variation. P Summarize data in two-way frequency tables. P 	 bar graph cumulative frequency distribution dot plot frequency table histogram joint frequencies linear transformation marginal frequencies mean measures of center median mode percentile qualitative data relative frequency skewed distribution standard deviation two-way frequency table